# Alkaline-Earth Squarates 

# V. Hydrogen Bonding in $\mathrm{BaC}_{4} \mathrm{O}_{\mathbf{4}} \cdot \mathbf{3} \mathrm{H}_{\mathbf{2}} \mathrm{O}$ : A Neutron Diffraction Study* 

CHRISTIAN ROBL $\dagger$<br>Institut für Anorganische Chemie der Universität München, Meiserstr. 1, D-8000 Munich 2, Federal Republic of Germany

and WERNER F. KUHS<br>Institut Max von Laue-Paul Langevin, 156X, F-38042 Grenoble Cedex, France

Received March 6, 1987; in revised form June 30, 1987


#### Abstract

Triclinic crystals of $\mathrm{BaC}_{4} \mathrm{O}_{4} \cdot 3 \mathrm{H}_{2} \mathrm{O}$ were grown in an aqueous silica gel. Lattice constants were $\mathfrak{a}=$ $660.38(9) \mathrm{pm}, b=859.83(8) \mathrm{pm}, c=878.26(9) \mathrm{pm}, \alpha=61.281(8)^{\circ}, \beta=63.827(9)^{\circ}, \gamma=70.53(1)^{\circ} ; Z=2$, space group $P \overline{1}$. Anisotropic refinement of neutron diffraction data led to $R_{w}=0.0234$ including anharmonic thermal parameters for H atoms. $\mathrm{Ba}^{2+}$ has $\mathrm{CN} 8+1$. It is surrounded by five water molecules and four $\mathrm{O}_{\text {squarate }}$ atoms ( $\mathrm{Ba}-\mathrm{O}$ 271.3-323.1 pm). The squarate dianion is almost planar and shows $\mathrm{C}-\mathrm{C}$ and $\mathrm{C}-\mathrm{O}$ bond lengths indicating the existence of undisturbed resonance stabilization, although one $\mathrm{O}_{\text {squarate }}$ atom is not connected to $\mathrm{Ba}^{21}$ ( $\mathrm{C}-\mathrm{O} 124.4-125.5 \mathrm{pm}, \mathrm{C}-\mathrm{C} 145.6-147.7 \mathrm{pm}$ ). Asymmetric hydrogen bonds between $\mathrm{H}_{2} \mathrm{O}$ and $\mathrm{O}_{\text {squarate }}$ play an important part in this structure. Obviously the bonding between $\mathrm{O}_{\text {squarate }}$ and its noncarbon neighbors is dominated by electrostatic and ionic interactions. © 1988 Academic Press, Inc.


## Introduction

Squaric acid (3,4-dihydroxycyclobut-3-ene-1,2-dione) is one of the so-called oxocarbon acids. Its dianion is strongly stabilized by resonance effects (2). Therefore its four oxygen atoms are to be regarded as equivalent and the dianion can act in principle as a fourfold monodentate ligand providing interesting applications in structural and coordination chemistry.

[^0]Many different types of inorganic squarates have already been studied, particularly by describing their crystal structures which often are of special interest (3, 4). Mostly polymeric complex compounds are formed, the most important of which show clathrate-, zeolite-like, or intercalation properties $(5-7)$.
$\mathrm{C}_{4} \mathrm{O}_{4}^{2-}$ was often found to be coordinated by less than its four oxygen atoms to the metal cations ( $8-12$ ). This, however, did not result in $\mathrm{C}-\mathrm{O}$ bond lengths differing sufficiently to allow discernment between the differently coordinated $\mathrm{O}_{\text {squarate }}$ atoms. Instead, the $\mathrm{C}-\mathrm{O}$ and $\mathrm{C}-\mathrm{C}$ distances were typical of completely delocalized $\pi$-elec-
trons indicating that the resonance effects remained essentially undisturbed. This surprising fact can be explained by taking the water of crystallization into consideration. Close distances between $\mathrm{H}_{2} \mathrm{O}$ and particularly those $\mathrm{O}_{\text {squarate }}$ atoms not bound to metal cations appear pointing to the existence of strong hydrogen bonds.

The crystal structure of $\mathrm{BaC}_{4} \mathrm{O}_{4} \cdot 3 \mathrm{H}_{2} \mathrm{O}$ is a good example. One $\mathrm{O}_{\text {squarate }}$ atom is bound to two $\mathrm{Ba}^{2+}$, two are coordinated by one $\mathrm{Ba}^{2+}$ each, and the fourth has no bonding contact with $\mathrm{Ba}^{2+}$. In order to shed light on the effects of hydrogen bonding in this compound we carried out a neutron diffraction study, the results of which are presented here.

## Experimental Details and Structure Refinement

Neutron diffraction data were recorded with a single crystal of $\mathrm{BaC}_{4} \mathrm{O}_{4} \cdot 3 \mathrm{H}_{2} \mathrm{O}$. The compound was obtained as colorless platelets from an aqueous silica gel according to Ref. (II).

Crystallographic and measuring details include the following: triclinic, $a=$ $660.38(9) \mathrm{pm}, \quad b=859.83(8) \mathrm{pm}, c=$ 878.26(9) pm, $\alpha=61.281(8)^{\circ}, \quad \beta=$ $63.827(9)^{\circ}, \gamma=70.53(1)^{\circ}, V=387.81 \times 10^{6}$ $\mathrm{pm}^{3}$ (calculated from single-crystal X-ray data, $293 \mathrm{~K}, \lambda=71.07 \mathrm{pm}$ ). The space group $P \overline{1}$ (No. 2) was confirmed by structure refinement and $E$ statistics. $Z=2$, $M_{r}=303.43, D_{x}=2.60 \mathrm{Mg} \mathrm{m}^{-3}$.

Neutron data collection was carried out using the following: D9B four circle diffractometer at the ILL, $296 \mathrm{~K}, \lambda=84.36 \mathrm{pm}$ ( H 3 beam tube), $\mathrm{Cu}(220)$ monochromator in transmission, $\lambda / 2$ contamination filtered by Erbium foil, $\mu=1.04 \mathrm{~cm}^{-1}$, crystal dimensions $3 \times 5 \times 1 \mathrm{~mm}$, numerical absorption correction, anisotropic extinction correction, $\omega-2 \theta$ scan, $\theta$ limit $42^{\circ}, 3580$ reflections recorded, 3225 unique, merging $R=$

TABLE I
Residuals after Refinement

| Type of <br> refinement | Number of <br> parameters | $R$ <br> (All reflec- <br> tions: | $R_{w}$ <br> Hanmonically | 163 | 0.0302 | 0.0263 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Haserved reflections <br> only: 2661) |  |  |  |  |  |  |
| anisoropic | 0.0207 | 0.0240 | 1.21 |  |  |  |
| H anharmonic <br> significant <br> $C^{i j k}$ only | 190 | 0.0296 | 0.0257 | 0.0201 | 0.0234 | 1.18 |
| H anharmonic <br> all $C^{i j k}$ | 223 | 0.0296 | 0.0256 | 0.0200 | 0.0233 | 1.18 |

0.0057 , refinement on $|F|$, quantity minimized $\Sigma w\left(\left|F_{\mathrm{o}}\right|-\left|F_{\mathrm{c}}\right|\right)^{2}$, weights $1 / \sigma_{|F|}^{2}$ from counting statistics, scattering lengths from Ref. (13), reflections with $I<3 \sigma_{I}$ considered as unobserved ( 2661 reflections observed).

Starting parameters for the refinements were obtained from the results of the X-ray structure determination (11). H positions were found in difference Fourier maps. For H atoms anharmonic thermal parameters were refined as well. The resulting probability density function was calculated by the Gram-Charlier expansion using third order moments (program system PROMETHEUS (14)). C $C^{i j k}$ not differing distinctly from their e.s.d.'s in preliminary refinements were set to zero during the final cycles. According to Hamilton (15) the refinement of third order moments leads to a reduction of $R_{w}$ which is better than the $0.5 \%$ significance level. The further improvement by introduction of all $C^{i j k}$ is not significant even at the $50 \%$ level (see Table I). Atom parameters are listed in Tables IIIV. Additional matcrial has bcen deposited with the NAPS. ${ }^{1}$

[^1]TABLE II
Parameters for $\mathrm{BaC}_{4} \mathrm{O}_{4} \cdot 3 \mathrm{H}_{2} \mathrm{O}$

| Atom | $X$ | $Y$ | Z | 11 | ${ }^{2}$ | ${ }^{3}$ | 号 | U | $U^{23}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Ba | 1474 | .18532(5) | 07304(5) | 0159(2) | .0125(2) | .0120(2) | -.0012(1) | -.0034(1) | -.0035(1) |
| W(1) | .76796(7) | .46701(6) | .01501(6) | . 0190 (2) | .0278(2) | .0193(2) | -.0029(1) | -.0053(1) | -.0102(2) |
| $W(2)$ | .36522(8) | .10281(6) | . $32402(6)$ | .0279(2) | .0210(2) | .0227(2) | -.0058(2) | -.0071(2) | -.0092(2) |
| W(3) | .82434(9) | .97024(8) | .20656(9) | .0244(2) | .0256(2) | .0514(3) | -.0072(2) | -.0026(2) | -.0169(2) |
| $\mathrm{O}(1)$ | .83804(9) | .19958(6) | .40884(6) | .0344(2) | .0210(2) | .0173(2) | -.0060(2) | -.0009(2) | -.0115(1) |
| $\mathrm{O}(2)$ | .15518(8) | . $37914(6)$ | .71967(5) | .0315(2) | .0180(2) | .0119(1) | -.0076(1) | -.0042(1) | -.0004(1) |
| O(3) | .35422(8) | .42957(6) | .29493(6) | .0298(2) | .0182(2) | .0178(2) | -.0050(1) | -.0034(1) | -.0098(1) |
| $\mathrm{O}(4)$ | . 38775 (7) | .84092(5) | .16234(5) | .0249(2) | .0138(2) | .0130(1) | -.0031(1) | -.0016(1) | -.0015(1) |
| C(1) | .21533(5) | .69916(4) | .51056(4) | .0175(1) | .0137(1) | .0115(1) | -.0023(1) | -.0021(1) | -.0051(1) |
| C(2) | .20932(5) | .50854(4) | .56910(4) | .0162(1) | .0135(1) | .0102(1) | -.0031(1) | -.0027(1) | -.0028(1) |
| C(3) | .30195(5) | .53084(4) | .37669(4) | .0164(1) | .0128(1) | . $0110(1)$ | -.0024(1) | -.0028(1) | -.0043(1) |
| C(4) | .31533(5) | .71828(4) | .31632(4) | .0157(1) | .0116(1) | .0105(1) | -.0016(1) | -.0021(1) | -.0032(1) |
| H(11) | .25851(28) | .51888(15) | .09194(14) | .0419(4) | .0421(5) | .0291(4) | -.0064(4) | -.0128(3) | $-.0166(3)$ |
| H(12) | .62297(17) | .44683(19) | .11712(14) | .0289(4) | .0414(4) | .0295(4) | -.0078(3) | -.0024(3) | -.0161(3) |
| H(21) | . $34535(23)$ | .20346(26) | .35345(18) | .0444(4) | .0335(4) | .0401(4) | -.0046(3) | $-.0140(4)$ | -.0206(4) |
| H(22) | .28736(28) | .00907(20) | .43472(15) | .0416(4) | .0345(4) | .0309(4) | -.0114(3) | -.0095(3) | $-.0071(3)$ |
| H(31) | .66284(33) | .01856(14) | .24828(27) | .0314(4) | .0396(5) | .0549(6) | -.0049(3) | -.0068(4) | $-.0231(4)$ |
| H(32) | .83322(21) | .84218(23) | .26664(16) | .0455(5) | .0319(4) | .0357(4) | -.0075(3) | -.0128(4) | -.0109(3) |

## Results and Discussion

The results of the previous X-ray structure determination are confirmed. $\mathrm{Ba}^{2+}$ is coordinated by four $\mathrm{O}_{\text {squarate }}$ atoms and five water molecules. One of the latter is much more remote than the others; therefore, CN is $8+1$ (see Tables $V$ and VI). Bond lengths and angles of the squarate dianion are shown in Table VII. They are in good agreement with the X-ray results. The
asymmetric environment of $\mathrm{C}_{4} \mathrm{O}_{4}^{2-}$ in this type structure leads to $\mathrm{C}-\mathrm{C}$ and $\mathrm{C}-\mathrm{O}$ bond lengths differing outside the limits of experimental error. However, there are no hints to any considerable disturbation of the $\pi$ electron delocalization. Furthermore the squarate dianion exhibits only slight deviations from planarity. The oxygen atoms are particularly bent out of plane in a bisphenoidal fashion which was observed in other squarate-type structures as well ( $5,8,10$,

TABLE III
$\mathrm{BaC}_{4} \mathrm{O}_{4} \cdot 3 \mathrm{H}_{2} \mathrm{O}$ : Anharmonic Temperature Factor Coefficients (Gram-Charlier Expansion)

| Atom | $C^{111}$ | $C^{222}$ | $C^{333}$ | $C^{112}$ | $C^{122}$ | $C^{113}$ | $C^{133}$ | $C^{223}$ | $C^{233}$ | $C^{123}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathrm{H}(11)$ | $-.40(12)$ | 0 | 0 | 0 | $.14(5)$ | 0 | $.14(4)$ | 0 | 0 | $-.08(3)$ |
| $\mathrm{H}(12)$ | 0 | $-.06(6)$ | 0 | 0 | $.03(4)$ | $.05(4)$ | 0 | 0 | 0 | 0 |
| $\mathrm{H}(21)$ | 0 | $-.14(7)$ | 0 | $-.13(6)$ | $-.06(5)$ | 0 | $.15(4)$ | $.18(5)$ | $-.16(4)$ | 0 |
| $\mathrm{H}(22)$ | $.37(15)$ | $.24(6)$ | 0 | 0 | $-.21(5)$ | $-.16(6)$ | 0 | 0 | 0 | $.13(3)$ |
| $\mathrm{H}(31)$ | $-.32(15)$ | 0 | $-.13(9)$ | 0 | 0 | $.12(8)$ | $.14(7)$ | 0 | 0 | 0 |
| $\mathrm{H}(32)$ | 0 | $.11(6)$ | 0 | $.26(7)$ | 0 | $-.12(7)$ | $.14(5)$ | 0 | 0 | $-.11(3)$ |

Note. Multiplied by $10^{5}$; coefficients not significantly greater than e.s.d.'s were set to zero for final refinements.

TABLE IV
Mean Positions of H Along the
Covalent O-H Bond

| Atom | $X$ | $Y$ | $Z$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{H}(11)$ | .25869 | .51866 | .09234 |
| $\mathrm{H}(12)$ | .62223 | .44723 | .11699 |
| $\mathrm{H}(21)$ | .34510 | .20535 | .35245 |
| $\mathrm{H}(22)$ | .28723 | .00685 | .43525 |
| $\mathrm{H}(31)$ | .66212 | .01895 | .24837 |
| $\mathrm{H}(32)$ | .83222 | .84142 | .26650 |

12). Obviously this is due to repulsive interactions between the negatively charged oxygen atoms. A thermal motion analysis in terms of a rigid body model (TLS (16)) gave isotropic translational and librational components with almost insignificant helical motions; the coordinates of the origin which symmetrizes the $S$ tensor are 0.3138 , 0.6204 , and 0.3637 (compared to the center of gravity at $0.2629,0.6132$, and 0.4425 this position is shifted toward $C(3)$ and $C(4))$.

Interesting insights are provided by inspecting the system of hydrogen bonds. Each of the three crystallographically independent water molecules is involved in hydrogen bonding leading to six unique asymmetric hydrogen bonds. Thereof, five occur between $\mathrm{O}_{\text {squarate }}$ atoms and $\mathrm{H}_{2} \mathrm{O}$, but only one between water molecules (compare Fig. 1). $W(1)\left(W=\mathrm{H}_{2} \mathrm{O}\right)$ connects two centrosymmetrically related $\mathrm{C}_{4} \mathrm{O}_{4}^{2-}$ by hydrogen bonding to $\mathrm{O}(3)$. Two $\mathrm{C}_{4} \mathrm{O}_{4}^{2-}$ which are

TABLE V
Ba-O Distances
IN pm

| $\mathrm{Ba}-\mathrm{O}(2)$ | $271.3(1)$ |
| :--- | :--- |
| $\mathrm{Ba}-\mathrm{O}(4)$ | $276.3(1)$ |
| $\mathrm{Ba}-W(3)$ | $277.3(1)$ |
| $\mathrm{Ba}-\mathrm{O}(1)$ | $278.4(1)$ |
| $\mathrm{Ba}-W(2)$ | $283.6(1)$ |
| $\mathrm{Ba}-\mathrm{O}(4)^{\prime}$ | $285.2(1)$ |
| $\mathrm{Ba}-W(1)$ | $288.1(1)$ |
| $\mathrm{Ba}-W(1)^{\prime}$ | $289.1(1)$ |
| $\mathrm{Ba}-W(3)^{\prime}$ | $323.1(1)$ |

TABLE VI
Bond Angles Around $\mathrm{Ba}^{2+}$

|  |  |  |
| :---: | :---: | :---: |
| $A / B$ | Angles $A-\mathrm{Ba}-B$ <br> $\left({ }^{\circ}\right)$ | Distance $A-\bar{B}$ <br> $(\mathrm{pm})$ |
| $\mathrm{O}(2) / \mathrm{O}(4)$ | $118.42(2)$ | 470.4 |
| $\mathrm{O}(2) / W(3)^{a}$ | $100.74(3)$ | 422.5 |
| $\mathrm{O}(2) / \mathrm{O}(1)$ | $132.92(3)$ | 504.0 |
| $\mathrm{O}(2) / W(2)$ | $144.45(4)$ | 528.4 |
| $\mathrm{O}(2) / \mathrm{O}(4)^{\prime}$ | $72.47(2)$ | 329.1 |
| $\mathrm{O}(2) / W(1)$ | $63.08(2)$ | 293.0 |
| $\mathrm{O}(2) / W(1)^{\prime}$ | $75.89(2)$ | 344.8 |
| $\mathrm{O}(2) / W(3)^{\prime}$ | $53.61(2)$ | 272.0 |
| $\mathrm{O}(4) / W(3)$ | $75.99(3)$ | 340.8 |
| $\mathrm{O}(4) / \mathrm{O}(1)$ | $105.10(2)$ | 440.4 |
| $\mathrm{O}(4) / W(2)$ | $67.86(2)$ | 312.6 |
| $\mathrm{O}(4) / \mathrm{O}(4)^{\prime}$ | $65.73(2)$ | 304.8 |
| $\mathrm{O}(4) / W(1)$ | $157.96(4)$ | 554.0 |
| $\mathrm{O}(4) / W(1)^{\prime}$ | $135.16(4)$ | 522.7 |
| $\mathrm{O}(4) / W(3)^{\prime}$ | $71.89(2)$ | 353.9 |
| $W(3) / \mathrm{O}(1)$ | $72.04(3)$ | 326.8 |
| $W(3) / W(2)$ | $114.36(3)$ | 471.3 |
| $W(3) / \mathrm{O}(4)^{\prime}$ | $129.64(3)$ | 509.0 |
| $W(3) / W(1)$ | $82.12(3)$ | 371.5 |
| $W(3) / W(1)^{\prime}$ | $146.82(4)$ | 542.8 |
| $W(3) / W(3)^{\prime}$ | $64.41(3)$ | 322.3 |
| $\mathrm{O}(1) / W(2)$ | $67.47(3)$ | 312.2 |
| $\mathrm{O}(1) / \mathrm{O}(4)^{\prime}$ | $147.58(4)$ | 541.2 |
| $\mathrm{O}(1) / W(1)$ | $69.84(2)$ | 324.4 |
| $\mathrm{O}(1) / W(1)^{\prime}$ | $86.11(2)$ | 387.5 |
| $\mathrm{O}(1) / W(3)^{\prime}$ | $135.82(4)$ | 557.7 |
| $W(2) / \mathrm{O}(4)^{\prime}$ | $80.60(3)$ | 367.9 |
| $W(2) / W(1)$ | $125.22(3)$ | 507.6 |
| $W(2) / W(1)^{\prime}$ | $77.60(3)$ | 358.9 |
| $W(2) / W(3)^{\prime}$ | $138.26(3)$ | 567.1 |
| $\mathrm{O}(4)^{\prime} / W(1)$ | $129.93(2)$ | 519.5 |
| $\mathrm{O}(4)^{\prime} / W(1)^{\prime}$ | $81.54(3)$ | 375.0 |
| $\mathrm{O}(4)^{\prime} / W(3)^{\prime}$ | $73.17(3)$ | 363.9 |
| $W(1) / W(1)^{\prime}$ | $66.76(3)$ | 317.6 |
| $W(1) / W(3)^{\prime}$ | $96.44(3)$ | 456.4 |
| $W(1)^{\prime} / W(3)^{\prime}$ | $128.05(2)$ | 550.6 |
|  |  |  |
| $a$ |  |  |

${ }^{a} W=\mathrm{H}_{2} \mathrm{O}$.
equivalent due to translational symmetry are connected via $O(3)$ and $O(1)$ by $W(2)$. $W(3)$ is proton donator to $O(2)$ and $W(2)$. A rather complicated network results, if the connections between $\mathrm{Ba}^{2+}$ and the $\mathrm{O}_{\text {squarate }}$ atoms are taken into consideration (11).
It should be emphasized that $O(4)$ which is bound to $2 \mathrm{Ba}^{2+}$ does not participate in hydrogen bonding. $O(1)$ and $O(2)$ have one

TABLE VII
The Geometry of the $\mathrm{C}_{4} \mathrm{O}_{4}^{2-}$ Dianion

| $\mathrm{C}(1)-\mathrm{C}(2)$ | $147.2(1)$ | $\mathrm{C}(1)-\mathrm{O}(1)$ | $124.5(1)$ |
| :--- | ---: | :--- | ---: |
| $\mathrm{C}(2)-\mathrm{C}(3)$ | $145.7(1)$ | $\mathrm{C}(2)-\mathrm{O}(2)$ | $124.4(1)$ |
| $\mathrm{C}(3)-\mathrm{C}(4)$ | $145.6(1)$ | $\mathrm{C}(3)-\mathrm{O}(3)$ | $125.5(1)$ |
| $\mathrm{C}(4)-\mathrm{C}(1)$ | $147.7(1)$ | $\mathrm{C}(4)-\mathrm{O}(4)$ | $125.1(1)$ |
| $\mathrm{O}(1)-\mathrm{C}(1)-\mathrm{C}(2)$ | $135.27(4)$ | $\mathrm{O}(2)-\mathrm{C}(2)-\mathrm{C}(1)$ | $135.51(4)$ |
| $\mathrm{O}(1)-\mathrm{C}(1)-\mathrm{C}(4)$ | $135.46(4)$ | $\mathrm{O}(2)-\mathrm{C}(2)-\mathrm{C}(3)$ | $134.38(5)$ |
| $\mathrm{C}(2)-\mathrm{C}(1)-\mathrm{C}(4)$ | $89.26(3)$ | $\mathrm{C}(1)-\mathrm{C}(2)-\mathrm{C}(3)$ | $90.07(3)$ |
| $\mathrm{O}(3)-\mathrm{C}(3)-\mathrm{C}(2)$ | $134.98(4)$ | $\mathrm{O}(4)-\mathrm{C}(4)-\mathrm{C}(1)$ | $136.01(5)$ |
| $\mathrm{O}(3)-\mathrm{C}(3)-\mathrm{C}(4)$ | $134.28(4)$ | $\mathrm{O}(4)-\mathrm{C}(4)-\mathrm{C}(3)$ | $134.06(4)$ |
| $\mathrm{C}(2)-\mathrm{C}(3)-\mathrm{C}(4)$ | $90.73(3)$ | $\mathrm{C}(1)-\mathrm{C}(4)-\mathrm{C}(3)$ | $89.91(3)$ |

Equation of least-squares plane:

| $6.3813 x+0.7102 y$ | $+3.2540 z=3.5517$ |  |  |  |
| :---: | :---: | :---: | :---: | ---: |
| Deviations from plane (pm) | $C(1)$ | -1.97 | $O(1)$ | -2.61 |
|  | $C(2)$ | -0.30 | $O(2)$ | 4.96 |
|  | $C(3)$ | -2.21 | $O(3)$ | -2.65 |
|  | $C(4)$ | -0.01 | $O(4)$ | 4.81 |

Note. Bond lengths are given in picometers, angles in degrees.
proton neighbor each. $\mathrm{O}(3)$ which is not coordinated by $\mathrm{Ba}^{2+}$ is involved in three hydrogen bonds.

Using the anharmonic thermal parameters the mean positions along the $\mathrm{O}-\mathrm{H}$ bond were calculated for each H atom. These coordinates were employed in the calculation of bond lengths and angles involving H atoms. In this way, it was possible to compensate for systematic errors in the bond geometry as obtained in the usual


Fig. 1. System of hydrogen bonds in $\mathrm{BaC}_{4} \mathrm{O}_{4}$ $3 \mathrm{H}_{2} \mathrm{O}$. (Hydrogen bonds are denoted by thin lines; thick lines lend to the $\mathrm{Ba}^{2+}$, which is not shown; W , water oxygen.)
harmonic treatment as a result of librations and stretch anharmonicity of the H atoms. In Table VIII the $\mathrm{O}-\mathrm{H}$ bond lengths calculated by this method are compared with those obtained from the refined atomic coordinates of the anharmonic and the conventional harmonic treatment. The mean coordinates lead to bond distances in a range which is well known from the literature. $\mathrm{O}-\mathrm{H}$ distances calculated with the harmonically refined coordinates are some-

TABLE VIII
Water and Hydrogen Bonds

|  | Anharmonic refinement |  |  |
| :---: | :---: | :---: | :---: |
|  | With refined atomic coordinates | With mean positions of H along $\mathrm{O}-\mathrm{H}$ | With harmonically refined atomic coordinates |
| H(11)-W(1) | 97.4(2) | 97.7 | 97.5 |
| $\mathrm{H}(12)-W(1)$ | 97.7(2) | 98.0 | 97.7 |
| $\mathrm{H}(11)-\mathrm{O}(3)$ | 187.7(2) | 187.3 | 187.8 |
| $\mathbf{H}(12)-\mathrm{O}(3)$ | 176.6(2) | 176.3 | 176.6 |
| H(21)-W(2) | 97.1(3) | 98.1 | 97.4 |
| $\mathbf{H}(22)-W(2)$ | 97.0(2) | 98.2 | 97.3 |
| $\mathrm{H}(21)-\mathrm{O}(3)^{\prime \prime}$ | $177.1(3)$ | 175.8 | 176.7 |
| $\mathrm{H}(22)-\mathrm{O}(1)$ | 184.7(2) | 183.1 | 184.3 |
| H(31)-W(3) | 97.5(3) | 98.0 | 97.4 |
| H(32)-W(3) | 95.9(2) | 96.5 | 96.4 |
| H(31)-W(2) | 178.6(3) | 178.2 | 178.7 |
| H(32)-O(2) | 182.6(3) | 181.7 | 182.1 |

All further distances and angles involving H have been calculated using the mean positions of H along $\mathrm{O}-\mathrm{H}$.

| $\mathrm{H}(11)-W(1)-\mathrm{H}(12)$ | $106.06(20)$ | $W(1)-\mathrm{H}(11)-\mathrm{O}(3)^{\prime}$ | $164.03(16)$ |
| :--- | :---: | :--- | :--- |
| $\mathrm{H}(11)-W(1)-\mathrm{Ba}$ | $109.27(13)$ | $W(1)-\mathrm{H}(12)-\mathrm{O}(3)$ | $175.63(18)$ |
| $\mathrm{H}(11)-W(1)-\mathrm{Ba}^{\prime}$ | $104.88(11)$ |  |  |
| $\mathrm{H}(12)-W(1)-\mathrm{Ba}$ | $115.59(11)$ | $W(1)-\mathrm{O}(3)$ | $274.1(1)$ |
| $\mathrm{H}(12)-W(1)-\mathrm{Ba}^{\prime}$ | $107.05(13)$ | $W(1) \mathrm{O}^{\prime}(3)^{\prime}$ | $282.6(1)$ |
| $\mathrm{Ba}-W(1)-\mathrm{Ba}^{\prime}$ | $\underline{113.24(4)}$ |  |  |
|  | $0=109.35$ |  |  |
| $\mathrm{H}(21)-W(2)-\mathrm{H}(22)$ | $109.97(15)$ | $W(2)-\mathrm{H}(21)-\mathrm{O}(3)^{\prime \prime}$ | $154.16(12)$ |
| $\mathrm{H}(21)-W(2)-\mathrm{Ba}$ | $112.53(15)$ | $W(2)-\mathrm{H}(22)-\mathrm{O}(1)$ | $162.61(17)$ |
| $\mathrm{H}(21)-W(2)-\mathrm{H}(31)$ | $108.94(20)$ |  |  |
| $\mathrm{H}(22)-W(2)-\mathrm{Ba}$ | $103.20(17)$ | $W(2)-\mathrm{O}(3)^{\prime \prime}$ | $267.5(1)$ |
| $\mathrm{H}(22)-W(2)-\mathrm{H}(31)$ | $108.61(17)$ | $W(2)-\mathrm{O}(1)$ | $278.4(1)$ |
| $\mathrm{H}(31)-W(2)-\mathrm{Ba}$ | $\underline{113.38(8)}$ |  |  |
|  | $0=109.44$ |  |  |
| $\mathrm{H}(31)-W(3)-\mathrm{H}(32)$ | $105.54(21)$ | $W(3)-\mathrm{H}(31)-W(2)$ | $178.45(25)$ |
| $\mathrm{H}(31)-W(3)-\mathrm{Ba}$ | $118.95(16)$ | $W(3)-\mathrm{H}(32)-\mathrm{O}(2)$ | $154.49(15)$ |
| $\mathrm{H}(31)-W(3)-\mathrm{Ba}$ | $102.73(17)$ |  |  |
| $\mathrm{H}(32)-W(3)-\mathrm{Ba}$ | $130.82(18)$ | $W(3)-W(2)$ | $276.1(1)$ |
| $\mathrm{H}(32)-W(3)-\mathrm{Ba}$ | $70.10(11)$ | $W(3)-\mathrm{O}(2)$ | $272.0(1)$ |
| $\mathrm{Ba}-W(32)-\mathrm{Ba} a^{\prime}$ | $\underline{115.59(3)}$ |  |  |
|  | $0=107.29$ |  |  |
|  |  |  |  |

Note. $\mathrm{Ba}^{\prime}$ refers to the longer $\mathrm{Ba}-\mathrm{W}$ distance. $W=$ water oxygen. Distances are given in picometers, angles in degrees.

TABLE IX
Surrounding of $\mathrm{O}_{\text {squarate }}$ Atoms

| $\mathrm{C}(1)-\mathrm{O}(1)-\mathrm{Ba}$ | 135.81(5) | $\mathrm{C}(2)-\mathrm{O}(2)-\mathrm{Ba}$ | $151.15(6)$ |
| :---: | :---: | :---: | :---: |
| $\mathrm{C}(1)-\mathrm{O}(1)-\mathrm{H}(22)$ | 111.02(6) | $\mathrm{C}(2)-\mathrm{O}(2)-\mathrm{H}(32)$ | 121.92(5) |
| $\mathrm{Ba}-\mathrm{O}(1)-\mathrm{H}(22)$ | 112.38(6) | Ва-O(2)-H(32) | 81.78(5) |
|  | $\theta=119.74$ |  | $0=118.28$ |
| $\mathrm{C}(3)-\mathrm{O}(3)-\mathrm{H}(11)$ | 117.167) | $\mathrm{C}(4)$-O(4)-Ba | $121.35(4)$ |
| $\mathrm{C}(3)-\mathrm{O}(3)-\mathrm{H}(12)$ | 114.22(9) | $\mathrm{C}(4)-\mathrm{O}(4)-\mathrm{Ba}^{\prime}$ | 122.19(5) |
| $\mathrm{C}(3)-\mathrm{O}(3)-\mathrm{H}(21)$ | 138.05 (6) | $\mathrm{Ba}-\mathrm{O}(4)-\mathrm{Ba}{ }^{\text {a }}$ | 114.27(2) |
| $\mathrm{H}(11)-\mathrm{O}(3)-\mathrm{H}(12)$ | 80.57(9) | - - 119.27 |  |
| $\mathrm{H}(11)-\mathrm{O}(3)-\mathrm{H}(21)$ | 93.60 (10) |  |  |
| $\mathrm{H}(12)-\mathrm{OH}(3)-\mathrm{H}(21)$ | 97.58 (10) |  |  |
| $0=106.86$ |  |  |  |
| Least-squares planes: |  |  |  |
| Plane I $\mathrm{C}(1), \mathrm{C}(2), \mathrm{C}(3), \mathrm{C}(4), \mathrm{O}(1), \mathrm{O}(2), \mathrm{O}(3), \mathrm{O}(4)$ |  |  |  |
| Equation and deviation see Table VII |  |  |  |
| Plane II C(2), O(2), Ba, H(32) |  |  |  |
| Equation: $5.9019 x-0.3519 y+0.4002 z=1.2043$ |  |  |  |
| Deviations in pm: $\mathrm{C}(2) 7.98, \mathrm{O}(2)-13.39, \mathrm{Ba} 3.04, \mathrm{H}(32) 2.37$ |  |  |  |
| Plane III C(1), O(1), $\mathrm{Ba}, \mathrm{H}(22)$ |  |  |  |
| Equation: $5.7711 x-0.0515 y+5.0860 z=3.8361$ |  |  |  |
| Deviations in pm: $\mathrm{C}(1)-3.27, \mathrm{O}(1) 6.40, \mathrm{Ba}-1.47, \mathrm{H}(22)-1$. Plane IV C(4), $\mathrm{O}(4)$. $\mathrm{Ba}, \mathrm{Ba}^{\prime}$ |  |  |  |
|  |  |  |  |  |  |
| Equation: $4.7035 x+5.7866 y+8.0225 z=8.1115$ |  |  |  |
| Deviations in pm: $\mathrm{C}(4) 6.57, \mathrm{O}(4)-11.93$, Ba $2.71, \mathrm{Ba}^{\prime} 2.65$ |  |  |  |
| Angles between normals to the planes: |  |  |  |
| U/II 19.30 ${ }^{\circ}$, I/III 19.970 ${ }^{\text {a }}$ I/IV $53.65^{\circ}$ |  |  |  |

Note. Distances are given in picometers, angles in degrees; with mean positions of H along the covalent $\mathrm{O}-\mathrm{H}$ bond. $\mathrm{Ba}^{\prime}$ refers to the longer Ba-O distance.
what shorter than those obtained with the mean positions. Thus showing the dominance of the librations in the anharmonic deformations of the H atoms.

The somewhat short $W(3)-H(32)$ bond should be regarded in connection with the different $\mathrm{Ba}-W(3)$ distances. One distance is the greatest among all Ba -water bonds and the other is the shortest. A close $\mathrm{Ba}-$ $\mathrm{H}(32)$ distance also occurs (304.1(2) pm) whereas the other $\mathrm{Ba}-\mathrm{H}$ distances are much greater (the next shortest is $\mathrm{Ba}-\mathrm{H}(22)$ 320.6(2) pm).

The HOH angles differ considerably for the three water molecules. With $W(2)$ this angle is somewhat greater than the tetrahedron angle whereas with $W(1)$ and particularly $W(3)$ it well resembles the HOH angle in free water molecules. The surrounding of the water molecules is in good agreement with a tetrahedral arrangement of electron pairs (see Table VIII). Greater deviations are observed only with $W$ (3), but this has to
be considered with respect to the different $\mathrm{Ba}-W(3)$ distances.
The majority of the OHO angles are considerably bent. Only $W(3)-H(31)-W(2)$ and $W(1)-\mathrm{H}(12)-\mathrm{O}(3)$ are close to $180^{\circ}$.

The $\mathrm{C}-\mathrm{O}$ bond lengths are close to values known from $\mathrm{C}=0$ double bonds pointing to a rather efficient overlap between $p_{z}$ orbitals of C and $\mathrm{O}_{\text {squarate }}$ atoms. Assuming $s p^{2}$ hybridization of the $\mathrm{O}_{\text {squarate }}$ atoms, their noncarbon neighbors should be in plane with the $\mathrm{C}_{4} \mathrm{O}_{4}^{2-}$, if there is a considerable degree of covalent bonding. The corresponding interplane angles are listed in Table IX. With $O(1)$ and $O(2)$ this angle is about $20^{\circ}$, but the plane formed by $\mathrm{C}(4)$, $\mathrm{O}(4), \mathrm{Ba}$, and $\mathrm{Ba}^{\prime}$ is inclined to the $\mathrm{C}_{4} \mathrm{O}_{4}^{2-}$ plane by almost $54^{\circ} . \mathrm{O}(3)$ is surrounded by three H atoms and its $\mathrm{C}(3)$ neighbor even in an unusual and distorted tetrahedral fashion (see Fig. 2). Thus it is difficult to discuss the extent of covalency between the $\mathrm{O}_{\text {squarate }}$ atoms and their noncarbon neighbors. It seems that the bonding is more adequately described by assumption of ionic and electrostatic interactions.

In order to prove these considerations the study of hydrogen bonding in other squarates would be very helpful, preferably in structures containing cations with a stronger polarization than $\mathrm{Ba}^{2+} . \mathrm{ZnC}_{4} \mathrm{O}_{4}$. $4 \mathrm{H}_{2} \mathrm{O}$ (12), which shows two $\mathrm{O}_{\text {squarate }}$ atoms bound to $\mathrm{Zn}^{2+}$ and the other two obviously involved in strong hydrogen bonds, should be very suitable for this purpose.


Fig. 2. $\mathrm{O}(3)$ is surrounded by three protons and its $C(3)$ neighbor in a distorted tetrahedral fashion.

## Acknowledgments

C.R. is indebted to the ILL for financial support and allocation of beam time (Exp. No. 5-13-155). The generous support by Prof. Dr. Dr.h.c. Armin Weiss is gratefully acknowledged.

## References

I. C. Robl, V. Gnutzmann, and A. Weiss, $Z$. Anorg. Allg. Chem. 549, 187 (1987).
2. R. West and D. L. Powell, J. Amer. Chem. Soc. 85, 2577 (1963).
3. E. Riegler, Dissertation, University of München, Munich (1979).
4. C. Robl, Dissertation, University of München, Munich (1984).
5. A. Weiss, E. Riegler, and C. Robl, Z. Naturforsch. B Anorg. Chem. Org. Chem. 41, 1329 (1986).
6. A. Weiss, E. Riegler, and C. Robl, Z. Naturforsch. B Anorg. Chem. Org. Chem. 41, 1333 (1986).
7. C. Robl and A. Weiss, Mater. Res. Bull. 22, 373 (1987).
8. C. Robl and A. Weiss, Z. Naturforsch. B Anorg. Chem. Org. Chem. 41, 1341 (1986).
9. J. A. C. van Oolien, J. Reedijk, and A. L. Spek, Inorg. Chem. 18, 1184 (1979).
10. C. Robl and A. Weiss, Z. Naturforsch. B Anorg. Chem. Org. Chem. 41, 1490 (1986).
11. C. Robl and A. Weiss, $Z$. Naturforsch. B Anorg. Chem. Org. Chem. 41, 1485 (1986).
12. A. Weiss, E. Riegler, I. Alt, H. Boehme, and C. Robl, Z. Naturforsch. B Anorg. Chem. Org. Chem. 41, 18 (1986).
13. L. Koester and H. Rauch, "Summary of Neutron Scattering Lengths," IAEA Contract 2517/ RB (1981).
14. U. H. Zucker, E. Perenthaler, W. F. Kuhs, R. Bachmann, and H. Schulz, J. Appl. Crystallogr. 16, 358 (1983).
15. W. C. Hamilton, Acta Crystallogr, 18, 502 (1965).
16. V. Schomaker and K. N. Trueblood, Acta Crystallogr. Sect. B 24, 63 (1968).


[^0]:    * For part IV, see Ref. (I). Dedicated with best wishes to Prof. Dr. Dr.h.c. Armin Weiss on the occasion of his 60th birthday.
    $\dagger$ To whom correspondence should be addressed.

[^1]:    ${ }^{1}$ See NAPS Document No. 04537 for 19 pages of supplementary materials from ASIS/NAPS, Microfiche Publications, P.O. Box 3513, Grand Central Station, New York, NY 10163. Remit in advance $\$ 4.00$ for microfiche copy or for photocopy, $\$ 7.75$ up to 20 pages plus $\$ .30$ for each additional page. All orders must be prepaid.

